



# Plug-and-play diagnosis with limited model information



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## 1 Introduction

This project focuses on interconnected systems with  $N$  subsystems  $S_i$  controlled by  $N$  decentralised control stations  $C_i$ . It considers the local detection of a fault  $f$  which can occur in subsystem  $S_1$  taking into account that the fault has also effects on the other subsystems through the physical couplings (Fig. 1).

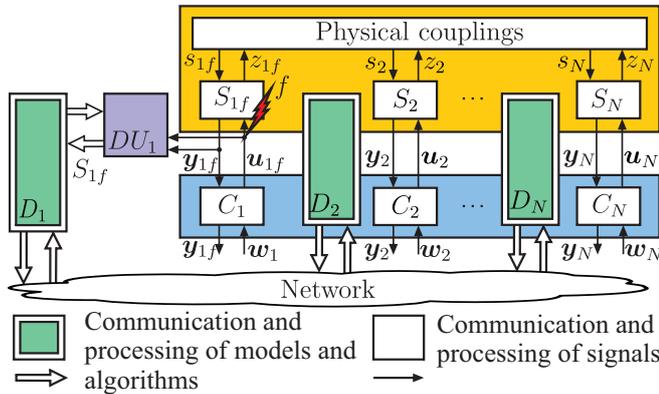


Figure 1: Plug-and-play diagnosis

Plug-and-play diagnosis is described here as a concept to organise the design steps of a local diagnostic unit without having a global coordinator available. In line with this concept, there exist  $N$  identical design agents  $D_i$  (double framed boxes in Fig. 1) which are assigned to the respective subsystem  $S_i$ . Each design agent stores the local models  $S_i$  and  $C_i$  of the corresponding subsystem and control station as well as the information about the couplings.

The design agent  $D_1$  organises the design steps of the diagnostic unit  $DU_1$ , which particularly consists of a model-based residual generation and a residual evaluation in order to detect the fault. Accordingly, based on the initially available information, the design agent  $D_1$  has to procure the models from other design agents  $D_i$  (double arrows in Fig. 1) to set-up a model with input  $\mathbf{u}_{1f}(t)$  and output  $\mathbf{y}_{1f}(t)$  that is used for the residual generation. In a second step, the design agent  $D_1$  has to fix a detection threshold to guarantee the detection of the fault.

In summary, the project is devoted to the question:

*Which models have to be communicated among the design agents  $D_i$  over the network so as to enable the design agent  $D_1$  to design a local diagnostic unit?*

Previous projects have dealt with plug-and-play reconfiguration as a concept to organise the reconfiguration of

$C_1$  without a global coordination [1, 2]. By the combination of plug-and-play reconfiguration and plug-and-play diagnosis a comprehensive fault-tolerant control scheme for interconnected systems is created.

## 2 Limit the model information

From the local perspective of the design agent  $D_1$  the faulty system with input  $\mathbf{u}_{f1}$  and output  $\mathbf{y}_{f1}$  consists of the faulty subsystem  $S_{1f}$

$$S_{1f}: \begin{cases} \mathbf{y}_{1f}(t) = \mathbf{S}_{yu1f}(t) * \mathbf{u}_{1f}(t) + \mathbf{S}_{ys1f}(t) * s_{1f}(t) \\ z_{1f}(t) = \mathbf{S}_{zu1f}^T(t) * \mathbf{u}_{1f}(t) + S_{zs1f}(t) * s_{1f}(t) \end{cases}$$

and of all controlled subsystems  $F_i|_{w_i=0}$ , ( $i=2, \dots, N$ )

$$F_i|_{w_i=0}: z_i(t) = F_{zsi}(t) * s_i(t) \quad (1)$$

illustrated in Fig. 2. In this project a local interconnection structure is considered, represented by the interconnection model

$$K: \begin{pmatrix} s_{f1}(s) \\ s_2(s) \\ \vdots \\ s_N(s) \end{pmatrix} = \begin{pmatrix} 0 & l_{12} & \dots & 0 \\ l_{21} & 0 & \ddots & 0 \\ \vdots & \ddots & 0 & l_{N-1N} \\ 0 & 0 & l_{NN-1} & 0 \end{pmatrix} \cdot \begin{pmatrix} z_{f1}(s) \\ z_2(s) \\ \vdots \\ z_N(s) \end{pmatrix}.$$

Due to this coupling structure, the dynamics of the faulty system can essentially be characterised by the dynamics of  $S_{1f}$  and of some controlled subsystems  $F_i|_{w_i=0}$ , ( $i=2, \dots, w-1$ ) combined to the model  $P_{1f}$ , shown in Fig. 2. In contrast to this, the dynamics of the other controlled subsystems  $F_i|_{w_i=0}$ , ( $i=w, \dots, N$ ) have a negligible influence and are combined to the error system

$$E_1: q_1(t) = E_1(t) * p_1(t).$$

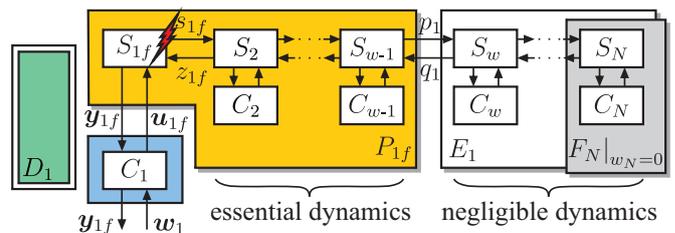


Figure 2: Limit the model information for diagnosis

To limit the amount of model information for diagnosis, the dynamics  $F_{zsi}(t)$ , ( $i=w, \dots, N$ ) of (1) are only known as upper bounds  $\bar{F}_{zsi}(t) \geq |F_{zsi}(t)|$ . The combination of these upper bounds yields an upper bound on the error dynamics  $\bar{E}_1(t) \geq |E_1(t)|$ .

Without a global coordinator, the design agent  $D_1$  initially knows only the local model  $S_{1f}$ ,  $C_1$  and  $K$ . Hence,  $D_1$  has to search for the relevant models  $F_i|_{w_i=0}$  and has to gather these models through the network using Alg. 1.

### 3 Local diagnosis

The local diagnostic unit  $DU_1$  consists of a residual generation and a residual evaluation described in the following.

The residual generator only makes use of the relevant models, combined in the model  $P_1$ . The residual generator denoted by  $O_1$  is represented by the I/O-oriented model

$$O_1 : \mathbf{r}_1(t) = \mathbf{O}_{ru1}(t) * \mathbf{u}_1(t) + \mathbf{O}_{ry1}(t) * \mathbf{y}_1(t). \quad (2)$$

As there is neither a global models available for the residual generation nor for the analysis of the residual, there exists a residual  $\mathbf{r}_1(t)$  in the fault-free case, which is only known to be located in a tube

$$|\mathbf{r}_1(t)| \in \mathbb{T}_1(t) = [\mathbf{0}, \bar{\mathbf{r}}_{\Delta 1}(t)].$$

The tube can be determined by the connection of the locally known models  $P_1$ ,  $C_1$ ,  $\bar{E}_1$  and  $O_1$ . Similarly, in the faulty case, a tube around the residual  $\mathbf{r}_{1f}(t)$  results to

$$|\mathbf{r}_{1f}(t)| \in \mathbb{T}_{1f}(t) = \left[ \max(\mathbf{0}, |\hat{\mathbf{r}}_{1f}(t)| - \bar{\mathbf{r}}_{\Delta 1f}(t)), |\hat{\mathbf{r}}_{1f}(t)| + \bar{\mathbf{r}}_{\Delta 1f}(t) \right]$$

from the analysis of the combination of the models  $P_{1f}$ ,  $C_1$ ,  $\bar{E}_1$  and  $O_1$ .

Both tubes  $\mathbb{T}_1(t)$  and  $\mathbb{T}_{1f}(t)$  are known by  $D_1$  during the design process of the diagnostic unit. From the evaluation of these tubes, the next theorem has been derived in [3].

**Theorem 1. (Guaranteed fault detection with limited model information)** Consider the residual generator (2). There exists a constant detection threshold  $\mu$ , if

1. the fault is detectable with limited model information

$$\exists t \in [t_f, \infty) : \mathbb{T}_{1f}(t) \cap \mathbb{T}_1(t) = \emptyset, \quad (3)$$

2. a false alarm is avoided

$$\exists t \in [t_f, \infty) : \mathbb{T}_{1f}(t) > \max_t \mathbb{T}_1(t). \quad (4)$$

Consequently, the fault is detected online, if

$$|\mathbf{r}_{1f}(t)| > \mu =: \max_t \mathbb{T}_1(t). \quad (5)$$

### 4 Plug-and-play diagnosis of a multizone furnace

This section proposes the organisation steps  $D_1$  has to perform in order to design the local diagnostic unit. It is shown that  $D_1$  can decide with locally available model information whether the model  $F_i|_{w_i=0}$  is relevant or not.

The procedure is applied to a multizone furnace, which consists of four locally interconnected heating zones shown in Fig. 3. The considered fault is a reduced actuator action in zone 1, modelled by  $S_{1f}$ . To design the local diagnostic unit  $DU_1$ , the design agent  $D_1$  runs Alg. 1.



Figure 3: Multizone furnace

#### Algorithm 1. (Plug-and-play diagnosis by $D_1$ )

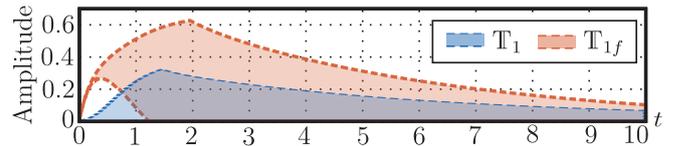
- Given: •  $D_1$  knows  $S_1, C_1, K$  and  $S_{1f}$   
•  $D_i$  knows  $S_i, C_i$ , ( $i = 2, \dots, N$ )

Proceed at  $D_1$ :

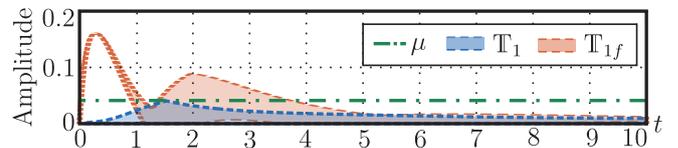
1. Procure upper bounds: Request  $\bar{F}_{zsi}(t) \geq |F_{zsi}(t)|$  from  $D_i$ , ( $i = 2, \dots, N$ ) and set  $k = 2$
2. Design  $O_1$  and determine  $\mathbb{T}_1(t)$  and  $\mathbb{T}_{1f}(t)$
3. Check the condition (3) and (4). If the conditions are satisfied, then choose  $\mu$  in accordance with (5) and STOP ( $DU_1$  exists), else goto 4.
4. If  $k \leq N$ , then  $D_k$  transmits the local models  $S_k, C_k$  through the network to  $D_1$ ,  $k = k + 1$  and goto 2., else STOP ( $DU_1$  does not exist).

Result: Local diagnostic unit  $DU_1$ .

At Step 1, the upper bounds are gathered from the design agents  $D_i$ , ( $i = 2, 3, 4$ ) so as  $D_1$  can design the residual generator  $O_1$  and can analyse the tubes (Step 2). Fig. 4(a) shows that although the fault is detectable, no constant detection threshold exists. Hence,  $D_1$  requests the model  $F_2|_{w_2=0}$  from  $D_2$  (Step 4) and redesigns  $O_1$  considering the neighbouring subsystem's dynamics. For this case, the tubes are shown in Fig. 4(b). It can be seen, that by using only the model of zone 2, the considered fault can be detected by a constant detection threshold  $\mu$ .



(a) Tubes from the exact models of  $D_1$



(b) Tubes from the exact models of  $D_1$  and  $D_2$

Figure 4: Resulting tubes during the design process

### References

- [1] S. Bodenburg, D. Vey and J. Lunze. Plug-and-play reconfiguration of decentralised controllers of interconnected systems. In *Proc. 9th Symp. on Fault Detection, Supervision and Safety of Technical Processes*, 2015, pp. 353–359.
- [2] S. Bodenburg and J. Lunze. Plug-and-play reconfiguration of locally interconnected systems with limited model information. In *Proc. 5th IFAC Workshop on Distributed Estimation and Control in Networked Systems*, 2015, pp. 20–27.
- [3] S. Bodenburg, and J. Lunze. Plug-and-play diagnosis of locally interconnected systems with limited model information. In *Proc. 3rd Conference on Control and Fault-Tolerant Systems*, 2016, (submitted).